one would have to assume the existence of a principal three-dimensional subgroup which is defined over K.

5. We note finally that if $\Gamma \subset G(K)$ satisfies the conditions of Corollary 1 to Theorem 2 and if H is a subgroup of maximal rank of G whose identity component is solvable, then for any $x \in G(K)/H(K)$, the isotropy group Γ_x is commutative, since its intersection with the isotropy group of x in $G(K)$ is on one hand free, as a subgroup of Γ, and on the other hand contains a solvable normal subgroup of finite index, since $H(K)$ does.

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