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Bestvina-Feighn theorem is given for mapping-tori of surface groups, the last one gives, thanks to [26], a new proof of the full version of the Combination Theorem for mapping-tori of hyperbolic groups, namely: "If  $G$  is a hyperbolic group and  $\alpha$  is a hyperbolic automorphism of  $G$ , then  $G \rtimes_{\alpha} \mathbf{Z}$  is a hyperbolic group."

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