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The Norm, its Variations, their Calculation and Relationships

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With 2 tables in the text

Abstract

Systematic differences between the standard C.I.P.W. weight percent norm, the Niggli catanorm and the volume norm are presented. Complete rules are given for their calculation and conversions. Rules are given for a weight percent norm which includes biotite and hornblende and its conversion to the mesonorm and volume norm. The appropriate application of the various norms is discussed.

INTRODUCTION

The norm is a powerful petrographic tool which is especially valuable for describing and classifying volcanic rocks which are not wholly crystalline. It is customary for petrologists to recalculate rock analyses to a norm. Resulting from this practice it has been found that variation diagrams of rock suites are better constructed on a norm-dependant parameter such as the differentiation index of THORNTON and TUTTLE (1960) or the crystallization index of POLDER-VAART and PARKER (1964) rather than on a weight percent parameter derived from the chemical analysis.

There are three major norm variations: the C.I.P.W. weight percent norm (JOHANNSEN, 1931), the Niggli catanorm (BARTH, 1962a) and the mesonorm (BARTH, 1962b). The C.I.P.W. norm is generally universally preferred by North American petrologists and the catanorm by European. The mesonorm is a special variation which has particular application to selected rocks. Because of tradition, very few petrologists are familiar with each of the norm variations. This article shows that the norm variations are very simply related and can be readily converted one to the other.

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THE C.I.P.W. NORM

The original norm is that of C. W. Cross, J. P. Iddings, L. V. Pirsson and H. S. Washington. The first complete compilation of the rules for its calculation was given by JOHANNSEN (1931) but it is only when faced with writing the rules logically for computer calculation that an unambiguous set of rules became available. KELSEY (1965) gave such a set of rules. Even then, they contain a few ambiguities which have been removed by the present author. A definitive set of C.I.P.W. rules is given in the appendix to this paper in a form readily convertable to computer language and capable of being applied by any person who can reliably perform simple arithmetic. A few improvements have been made to facilitate subsequent calculation of the crystallization index.

Meaning: The C.I.P.W. norm is an expression of the total rock chemistry in terms of the selected normative minerals expressed in *weight proportions* of the minerals. If the norm is finally recalculated to 100% anhydrous, as is common practice for better comparison, then the norm gives the weight % of the normative minerals.

The basis of the C.I.P.W. norm is well illustrated by the equations used to effect desilification when, after forming diopside or hypersthene (rule 22 in the Appendix), it is found that an excessive molecular proportion of SiO_2 has been allocated.

(rule 24)	2 (MgO SiO ₂)	Ξ	2 MgO SiO ₂	+	SiO_2
	$2 \mathrm{EN}$	=	\mathbf{FO}	+	\mathbf{Q}
and similarly	$2 \mathrm{FS}$	=	\mathbf{FA}	+	\mathbf{Q}

In the norm, 2MgO (molecular proportion) is both equal to 2 EN or 1 FO, whereas SiO_2 is equal to EN, FS, FO, FA or Q (in the desilification rules, Q = D).

(rule 25)	CaO TiO2 SiO2 TN		CaO TiO ₂ PF	+ +	${siO_2} \ { m Q}$
(rule 26)	Na2O Al2O3 6 SiO2 AB	II	Na ₂ O Al ₂ O ₃ 2 SiO ₂ NE	+ +	4 SiO ₂ 4 Q
(rule 27)	K ₂ O Al ₂ O ₃ 6 SiO ₂ OR	H	$\begin{array}{c} \mathrm{K_{2}O} \ \mathrm{Al_{2}O_{3}} \ 4 \ \mathrm{SiO_{2}} \\ \mathrm{LC} \end{array}$	+ +	2 SiO ₂ 2 Q
(rule 28)	2 (CaO SiO ₂) 2 WO)	$2 \operatorname{CaO} \operatorname{SiO}_2$ CS	+ +	SiO ₂ Q
(rule 29)	2 (CaO MgO 2 SiO ₂) 2 Mg-DI	=	$2 \operatorname{CaO} \operatorname{SiO}_2$ CS	+ +	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
similarly	2 Fe-DI	=	\mathbf{CS}	+	FA + 2Q
(rule 30)	K ₂ O Al ₂ O ₃ 4 SiO ₂ LC		K ₂ O Al ₂ O ₃ 2 SiO ₂ KP	+ +	2 SiO ₂ 2 Q

The normative parameter differentiation index (THORNTON and TUTTLE, 1960) is defined based upon the C.I.P.W. norm and *not* on any other variation. Hence to avoid confusion it should not be calculated from any other norm. Similarly the crystallization index (POLDERVAART and PARKER, 1964) is based only on the C.I.P.W. norm. The C.I.P.W. norm may equally be referred to as the weight percent norm. It is appropriate to plot weight percent chemical parameters, such as $K_2O \%$, total alkali % etc., against normative parameters based on the C.I.P.W. norm and not the Niggli norm.

THE NIGGLI CATANORM

Originally evolved by P. Niggli, the first set of readily available rules were compiled by BARTH (1962a). A logical set of rules, suitable for computer programming, is given by HUTCHISON (1974).

Meaning: The catanorm expresses the total rock chemistry in terms of the selected normative minerals expressed in cation proportions. For example, an oversimplified norm which gives albite 50%, anorthite 50% means that the cation proportions of Na_{0.5} AlO_{1.5} 3 SiO₂ and CaO 2 AlO_{1.5} 2 SiO₂ are equal. Both normative minerals have a total of 5 cations per molecule. Hence the cation proportions can be calculated as:

in albite Na $\frac{1}{5}$ of 50 = 10. Al $\frac{1}{5}$ of 50 = 10. Si $\frac{3}{5}$ of 50 = 30. in anorthite Ca $\frac{1}{5}$ of 50 = 10. Al $\frac{2}{5}$ of 50 = 20. Si $\frac{2}{5}$ of 50 = 20.

Hence the total cation proportions are Na 10, Ca 10, Al 30, Si 50.

The catanorm is closer to a volume norm (= mode) than the C.I.P.W. norm. If all normative minerals had identical atomic structure so that their specific gravities depended only upon their cation contents, then the catanorm would represent a volume norm. However the specific gravity of a mineral is dependant not just on the cation content but also on detailed atomic structure, hence the catanorm is not exactly equal to the volume norm.

The basis of the catanorm can be illustrated by the equations used to effect desilification.

and

$\begin{array}{c} 2 \ (\mathrm{MgO}\ \mathrm{SiO}_2) \\ 4 \ \mathrm{EN} \\ (2 \times 2) \end{array}$	II II	$\begin{array}{c} 2 \text{ MgO SiO}_2\\ 3 \text{ FO}\\ (3 \times 1) \end{array}$	+ +	${{{\rm SiO}_2}}\ {{ m Q}}\ {{ m (1 imes 1)}}$
4 FS	=	3 FA	+	Q
CaO TiO2 SiO2 3 TN	H H	CaO TiO ₂ 2 PF	+ +	SiO2 Q
NaO _{0.5} AlO _{1.5} 3 SiO ₂ 5 AB	=	NaO _{0.5} AlO _{1.5} SiO ₂ 3 NE	+ +	2 SiO2 2 Q
(5 cations)		(3 cations)		(2 cations)

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	KO _{0.5} AlO _{1.5} 3 SiO ₂ 5 OR	II II	KO _{0.5} AlO _{1.5} 2 SiO ₂ 4 LC	+ +	${{ m SiO}_2} { m Q}$
	2 (CaO SiO ₂) 4 WO	H	$\begin{array}{c} 2 \text{ CaO SiO}_2\\ 3 \text{ CS} \end{array}$	+ +	${{ m SiO}_2} { m Q}$
and	2 (CaO MgO 2 SiO ₂) 8 Mg-DI 8 Fe-DI		2 CaO SiO2 3 CS 3 CS	+ + +	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
	KO _{0.5} AlO _{1.5} 2 SiO ₂ 4 LC		KO _{0.5} AlO _{1.5} SiO ₂ 3 KP	+ +	${{ m SiO}_2} { m Q}$

It is appropriate to plot cation proportions derived from the total rock analysis against normative parameters based on the Niggli and not the C.I.P.W. norm. Weight based oxides should be compared only with weight based normative parameters (C.I.P.W.), whereas molecular or cationic proportions should be compared with the cation based norm (catanorm).

THE BARTH MESONORM

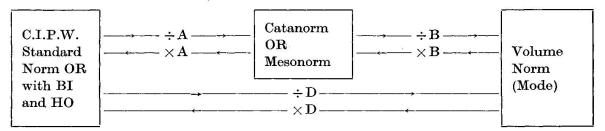
The rules for the mesonorm (a variation of the catanorm) were given by BARTH (1962b) and set out logically by HUTCHISON (1974). It is identical in meaning to the catanorm, and differs from it only in the introduction of the few minerals given in table 2. Because potassium is allocated to biotite, the normative amount of orthoclase (obtained by the catanorm) is reduced. Hornblende (actinolite + edenite + riebeckite) will also partly take the place of diopside and hypersthene. The mesonorm is suitable for granitic to dioritic rocks and for metamorphosed igneous rocks in which biotite and hornblende are more appropriate than diopside and hypersthene. The mesonorm or C.I.P.W. norm would do in forming diopside and hypersthene. Hence the mesonorm consistently has more Q, or for undersaturated rocks lesser amounts of undersaturated minerals than the other norms. These fundamental differences make the mesonorm more appropriate for granites, granodiorites, diorites and amphibolites.

SYSTEMATIC RELATIONSHIP BETWEEN THE NORMS

Conversion from the C.I.P.W. to the catanorm is relatively simple. Hence there is no real need to compute different norms independantly. A systematic scheme is given for conversion between the norms. Since the C.I.P.W. norm is perhaps the most widely used, it will be taken as the starting point, and complete rules for its calculation are given in the appendix. First choose whether to calculate the standard weight % C.I.P.W. norm or the modified weight % C.I.P.W. norm which includes biotite and hornblende. The choice will depend on whether an assemblage free of biotite and hornblende (e.g. basic igneous rocks) is more appropriate than one with biotite and hornblende (e.g. acid to intermediate igneous rocks and meta-igneous rocks). Having made the appropriate choice, calculate the C.I.P.W. norm according to the rules in the appendix. Normative-based parameters such as D.I. and C.I. must be based on the standard C.I.P.W. and not on the biotite-hornblende variation. It is best to end with an 100% anhydrous norm in which the total normative minerals is 100.

Table 1 gives the conversion factors required to change from the C.I.P.W. weight % norm to the catanorm (cation proportion norm) or a truly volume norm, which should be directly comparable with the mode (if the modal and normative minerals are identical). Likewise if we have already obtained a catanorm, it can be converted to a C.I.P.W. weight % or volume norm. A rock mode could be converted to a norm using the appropriate D factors. The conversion scheme is:

for each mineral in turn



Where the factors A, B, and D are given in Tables 1 and 2.

Then pro-rate to 100% by multiplying each mineral by $\frac{100 \times \text{mineral}}{\text{total of minerals}}$.

The conversion factors have been so calculated as to end with closely similar normative totals after conversion, so that the final proration to 100% results in only a very slight change in the amounts. The basis for the conversion is that a comparison of a large number of norms shows that orthoclase is closely similar in amount irrespective of which norm is calculated. Hence a conversion factor between C.I.P.W. and the catanorm for OR was taken as 1.000.

The derivation of the A, D, and B factors of table 1 is illustrated by an example. Factor A for albite = $\frac{30.99 + 50.98 + 3(60.08)}{5} \times \text{constant}$. The constant for all minerals is $\frac{5}{47.10 + 50.98 + 3(60.08)}$, so that all conversions are relative to orthoclase. D = $\frac{\text{the mineral specific gravity}}{2.57}$ (2.57 is the specific gravity of orthoclase). B = $\frac{D}{A}$.

Syr	nbol	Normative mineral	Cations	Formula	А	D	в
-	ic group						
	Q	quartz	1	SiO ₂	1.079	1.031	0.955
	č	corundum	ĩ	AlO _{1,5}	0.916	1.564	1.708
	Z	zircon	2	ZrO ₂ SiO ₂	1.646	1.821	1.106
	OR	orthoclase		KO _{0,5} AlO _{1,5} 3 SiO ₂	1.000	1.000	1.000
	AB	albite	5	NaO _{0.5} AlO _{1.5} 3 SiO ₂	0.942	1.019	1.082
	AN	anorthite	5	CaO 2 AlO _{1,5} 2 SiO ₂	1.000	1.074	1.074
	\mathbf{LC}	leucite	4	KO _{0,5} AlO _{1,5} 2 SiO ₂	0.980	0.965	0.985
	NE	nepheline	3	NaO _{0,5} AlO _{1,5} SiO ₂	0.851	1.012	1.189
	\mathbf{KP}	kalsilite	3	KO _{0.5} AlO _{1.5} SiO ₂	0.947	1.016	1.072
	\mathbf{HL}	halite	2	Na Ĉl	0.525	0.840	1.601
Fen	nic group						
	AC	acmite	4	NaO _{0.5} FeO _{1.5} 2 SiO ₂	1.037	1.381	1.331
	NS	sodium metasilica		$2 \operatorname{NaO}_{0.5} \operatorname{SiO}_2$	0.731	1.019	1.395
	KS	potassium meta-					
		silicate	3	$2 \text{ KO}_{0.5} \text{ SiO}_2$	0.924	1.070	1.158
	wo	wollastonite	2	CaO SiO ₂	1.043	1.109	1.063
	\mathbf{EN}	enstatite	2	MgO SiO ₂	0.902	1.249	1.385
	\mathbf{FS}	ferrosilite	2	FeO SiO ₂	1.185	1.541	1.300
	FO	forsterite	3	2 MgO SiO ₂	0.843	1.253	1.487
	\mathbf{FA}	fayalite	3	2 FeO SiO ₂	1.220	1.708	1.400
	\mathbf{CS}	larnite	3	2 CaO SiO ₂	1.031	1.288	1.249
	\mathbf{MT}	magnetite	3	FeO 2 FeO _{1,5}	1.387	2.016	1.454
	CM	chromite	3	FeO 2 CrO _{1.5}	1.340	1.981	1.478
	$\mathbf{H}\mathbf{M}$	hematite	1	FeO _{1.5}	1.435	2.043	1.424
	\mathbf{IL}	ilmenite	2	FeO TiO ₂	1.363	1.829	1.342
	\mathbf{TN}	\mathbf{sphene}	3	CaO TiO ₂ SiO ₂	1.174	1.362	1.160
	\mathbf{PF}	perovskite	2	CaO TiO ₂	1.221	1.568	1.284
	\mathbf{RU}	rutile	1	TiO ₂	1.435	1.634	1.139
	\mathbf{AP}	apatite	8	5 CaO 3 PO _{2,5}	1.108	1.265	1.142
	\mathbf{FR}	fluorite		CaO 2 F	0.563	1.237	2.196
	\mathbf{PR}	pyrite		FeO 2 S	0.814	1.953	2.399
	CC	calcite		CaO CO ₂	0.863	1.054	1.222
	\mathbf{CT}	cassiterite	1	SnO_2	2.707	2.724	1.006
an	∫Mg-SP	spinel	3	MgO 2 AlO _{1.5}	0.852	1.381	1.621
\mathbf{SP}	Fe-SP	hercynite		FeO 2 AlO _{1.5}	1.041	1.712	1.645
	(Mg-DI	diopside		CaO MgO 2 SiO ₂	0.973	1.253	1.288
\mathbf{DI}	Fe-DI	hedenbergite		CaO FeO 2 SiO ₂	0.975	$1.255 \\ 1.385$	1.288 1.243
	(10.01	noutiporgio	T	000 100 4 NIC2	1.114	1.909	1.440

Table 1. Normative minerals and conversion factors for the C.I.P.W. standard norm, the catanorm and the volume norm

Table 2. Additional normative minerals and conversion factors for the weight % norm (with
biotite and hornblende), the mesonorm and the volume norm

Sym	bol	Normative mineral	Cations	Formula	A	D	в
BI	$\begin{cases} Mg-BI \\ Fe-BI \end{cases}$	phlogopite annite	8 8	$\begin{array}{c} {\rm KO_{0.5}\ 3\ MgO\ AlO_{1.5}\ 3\ SiO_2} \\ {\rm KO_{0.5}\ 3\ FeO\ AlO_{1.5}\ 3\ SiO_2} \end{array}$	$0.897 \\ 1.109$	$\begin{array}{c} 1.074 \\ 1.167 \end{array}$	$\begin{array}{c} 1.197 \\ 1.052 \end{array}$
ACT	$egin{cases} Mg-ACT \ Fe-ACT \end{cases}$	tremolite ferro-actinolite		$\begin{array}{c} 2 \ {\rm CaO} \ 5 \ {\rm MgO} \ 8 \ {\rm SiO}_2 \\ 2 \ {\rm CaO} \ 5 \ {\rm FeO} \ 8 \ {\rm SiO}_2 \end{array}$	$\begin{array}{c} 0.951 \\ 1.140 \end{array}$		$\begin{array}{c} 1.236 \\ 1.175 \end{array}$
ED	$egin{cases} Mg-ED \ Fe-ED \end{cases}$	edenite ferro-edenite	$\begin{array}{c} 16\\ 16\end{array}$	$\begin{array}{l} \mathrm{NaO_{0.5}\ 2\ CaO\ 5\ MgO\ AlO_{1.5}\ 7\ SiO_2}\\ \mathrm{NaO_{0.5}\ 2\ CaO\ 5\ FeO\ AlO_{1.5}\ 7\ SiO_2} \end{array}$	$\begin{array}{c} 0.916 \\ 1.094 \end{array}$	$\begin{array}{c} 1.187 \\ 1.362 \end{array}$	$\begin{array}{c} 1.296 \\ 1.245 \end{array}$
	\mathbf{RI}	riebeckite	15	$2 \ \mathrm{NaO_{0.5}} \ 2 \ \mathrm{FeO_{1.5}} \ 3 \ \mathrm{FeO} \ 8 \ \mathrm{SiO_{2}}$	1.099	1.323	1.204
	in an and a second	weight the production of					

 $\mathbf{HO} = \mathbf{ACT} \!+\! \mathbf{ED} \!+\! \mathbf{RI}$

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Table 2 lists additional conversion factors which will be required if the norms containing biotite and hornblende are used. For these norms, the factors of table 1 apply and table 2 gives only the additional minerals needed.

The following are important fundamental differences and similarities between the norms:

- 1. The standard C.I.P.W. norm gives identical normative minerals to the catanorm, but the relative amounts differ. Where A of table 1 is close to 1.00, there will be little difference between the normative amounts. The greater the divergence from unity, the greater the normative difference. If A is less than unity, the amount in the catanorm will be greater than the amount in the C.I.P.W. norm and vice-versa.
- 2. Rock classifications based on norms, such as the basalt classification of YODER and TILLEY (1962) and GREEN and RINGWOOD (1967) should be equally valid based on either the C.I.P.W. or the catanorm, although they were defined on a C.I.P.W. basis.
- 3. Ratios in a mineral isomorphous series are properly calculated from the catanorm, e.g. plagioclase Ab_xAn_{100-x} , hypersthene En_xFS_{100-x} and olivine FO_xFA_{100-x} . The proportions of the end members obtained in the C.I.P.W. norm may be recalculated to cation proportions x and 100 x by using the factors A of table 1 without recalculation of the whole norm.
- 4. Relative plots of quartz, albite, orthoclase for granitic rocks are best based on mesonorm calculations because the C.I.P.W. standard norm over-allocates to the orthoclase molecule.

Appendix A: Rules for calculation of the standard C.I.P.W. weight % norm, crystallization and differentiation index

1. Calculate the amounts (molecular proportions) of the oxides and elements present in the analysis by dividing each given weight percentage by the appropriate following formula weight:

SiO ₂ 60.08	TiO ₂ 79.90	Al ₂ O ₃ 101.96	ZrO ₂ 123.22	${ m Fe_{2}O_{3}}$ 159.69	
MnO 70.94	FeO 71.85	NiO 74.71	MgO 40.31	BaO 153.34	CaO 56.08
SrO 103.62	Na ₂ O 61.98	Cr_2O_3 151.98	K ₂ O 94.20	Cl 35.45	SO ₃ 80.06
P ₂ O ₅ 141.94	F 19.00	CO ₂ 44.01	S 32.06	SnO ₂ 150.69	

- 2. Add the (MnO + NiO) amount to the FeO amount.
- 3. Add the (BaO + SrO) amount to the CaO amount.

In the following rules the oxides or elements referred to are the amounts obtained for them after applying rules 1 to 3 above. All normative minerals are taken as of zero amount until formed by the following rules applied consecutively.

4. Make $Z = ZrO_2$. Make Y = Z.

Throughout the norm calculation, amounts will be allocated to Y. The final total of Y is required at rule 23.

- 5. If CaO $\geq 10/3 P_2O_5$ Make AP = P₂O₅ Subtract 10/3 AP from CaO
- 6. If $F \ge 2/3$ AP Subtract 2/3 AP from F
- 7. If CaO ≥ 0.5 F Make FR = 0.5 F Subtract FR from CaO
- 8. If $Na_2O \ge 0.5$ Cl Make HL = Cl Subtract 0.5 HL from Na_2O
- 9. If FeO ≥ 0.5 S (or 0.5 SO₃) Make PR = 0.5 S (or 0.5 SO₃) Subtract PR from FeO
- 10. If $CaO \ge CO_2$ Make $CC = CO_2$ Reduce CaO by amount CC
- 11. If $FeO \ge Cr_2O_3$ Make $CM = Cr_2O_3$ Reduce FeO by amount CM
- 12. If $FeO \ge TiO_2$ Make IL = TiO_2 Reduce FeO by amount IL TiO_2 becomes zero
- 13. Make $CT = SnO_2$
- 14. If $Al_2O_3 \ge K_2O$ Make $OR = K_2O$ Reduce Al_2O_3 by amount ORIncrease Y by amount 6 OR

If CaO < $10/3 P_2O_5$ Make AP = 3/10 CaO Subtract AP from P₂O₅ CaO becomes zero Excess P_2O_5 weight % in rock $= 141.94 P_2O_5$ If F < 2/3 APMake F = zeroIf CaO < 0.5 FMake FR = CaO. Subtract 2 FR from F CaO becomes zero Excess F weight % in rock = 19.00 F If $Na_2O < 0.5$ Cl Make $HL = 2 Na_2O$ Subtract HL from Cl Na₂O becomes zero Excess Cl weight % in rock = 35.45 Cl If FeO < 0.5 S (or 0.5 SO₃) Make PR = FeOSubtract 2 PR from S (or SO₃) FeO becomes zero Excess S in weight % = 32.06 S (excess SO₃ in weight % = 80.06 SO₃) If $CaO < CO_2$ Make CC = CaOReduce CO₂ by amount CC CaO becomes zero Excess CO_2 weight % in rock = 44.01 CO_2 If FeO $< Cr_2O_3$ Make CM = FeOReduce Cr_2O_3 by amount CM FeO becomes zero Excess Cr₂O₃ weight % in rock $= 151.98 \,\mathrm{Cr}_2\mathrm{O}_3$ If $FeO < TiO_2$ Make IL = FeOReduce TiO₂ by amount IL FeO becomes zero If $Al_2O_3 < K_2O$ Make $OR = Al_2O_3$ Reduce K₂O by amount OR Al₂O₃ becomes zero Make $KS = K_2O$ Increase Y by amount (6 OR + KS)

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- 15. If $Al_2O_3 \ge Na_2O$ Make $AB = Na_2O$ Reduce Al_2O_3 by amount ABNa₂O becomes zero Increase Y by amount 6 AB
- 16. If $Na_2O \ge Fe_2O_3$ Make $AC = Fe_2O_3$ Fe_2O_3 becomes zero Reduce Na_2O by amount ACMake $NS = Na_2O$ Increase Y by amount (4 AC + NS)
- 17. If $Al_2O_3 \ge CaO$ Make AN = CaOCaO becomes zero Reduce Al_2O_3 by amount AN Increase Y by amount 2 AN Make $C = Al_2O_3$
- 18. If $CaO \ge TiO_2$ Make $TN = TiO_2$ Reduce CaO by amount TN Increase Y by amount TN
- 19. If $Fe_2O_3 \ge FeO$ Make MT = FeOFeO becomes zero Reduce Fe_2O_3 by amount MT Make $HM = Fe_2O_3$

If $Al_2O_3 < Na_2O$ Make $AB = Al_2O_3$ Reduce Na_2O by amount AB Al_2O_3 becomes zero Increase Y by amount 6 AB

If $Na_2O < Fe_2O_3$ Make $AC = Na_2O$ Reduce Fe_2O_3 by amount AC Increase Y by amount 4 AC

If $Al_2O_3 < CaO$ Make $AN = Al_2O_3$ Reduce CaO by amount AN Increase Y by amount 2 AN

If $CaO < TiO_2$ Make TN = CaOCaO becomes zero Reduce TiO_2 by amount TNMake $RU = TiO_2$ Increase Y by amount TN

If $Fe_2O_3 < FeO$ Make $MT = Fe_2O_3$ Reduce FeO by amount MT

20. Make (MgFe) = (MgO + FeO). Calculate $PrMg = \frac{MgO}{MgO + FeO}$ and $PrFe = \frac{FeO}{MgO + FeO}$

21. This rule is to be applied only if the weight percent of SiO_2 in the rock is less than 45.00 (that is the rock is ultrabasic). If SiO_2 weight % > 45.00, omit this rule and proceed to rule 22.

If $(MgFe) \leq C$ Make Mg:SP = PrMg (MgFe)Make Fe-SP = PrFe (MgFe)Reduce C by amount (Mg-SP + Fe-SP) (MgFe) becomes zero

22. If CaO \geq (MgFe) Make Mg-DI = PrMg (MgFe) Make Fe-DI = PrFe (MgFe) Reduce CaO by amount (Mg-DI + Fe-DI) If (MgFe) > C Make Mg-SP = PrMg (C) Make Fe-SP = PrFe (C) C becomes zero Reduce (MgFe) by amount (Mg-SP + Fe-SP)

If CaO < (MgFe) Make Mg-DI = PrMg (CaO) Make Fe-DI = PrFe (CaO) Reduce (MgFe) by amount (Mg-DI + Fe-DI) Make WO = CaO Increase Y by amount 2 (Mg-DI + Fe-DI) + WO

- 23. If $SiO_2 \ge Y$ Make $Q = SiO_2 - Y$ Omit rules 24 to 30 Go directly to rule 31
- 24. If $D \leq 0.5$ (EN + FS) Make FO = PrMg (D) Make FA = PrFe (D) Reduce EN by amount PrMg (2 D) Reduce FS by amount PrFe (2 D) D becomes zoro. Omit rules 25-30 Go directly to rule 31
- 25. If $D \leq TN$ Make PF = DReduce TN by amount D D becomes zero. Omit rules 26-30 Go directly to rule 31
- 26. If $D \leq 4 AB$ Make NE = D/4Reduce AB by amount D/4D becomes zero. Omit rules 27-30 Go directly to rule 31
- 27. If $D \leq 2 \text{ OR}$ Make LC = 0.5 DReduce OR by amount 0.5 D D becomes zero. Omit rules 28-30 Go directly to rule 31
- 28. If $D \leq 0.5$ WO Make CS = DReduce WO by amount 2 D D becomes zero. Omit rules 29–30 Go directly to rule 31
- 29. If $D \leq (Mg-DI + Fe-DI)$ Increase CS by amount 0.5 D Increase FO by amount 0.5 D (PrMg) Increase FA by amount 0.5 D (PrFe) Reduce Mg-DI by amount D (Pr-Mg) Reduce Fe-DI by amount D (PrFe) D becomes zero. Omit rule 30 Go directly to rule 31

Make EN = PrMg (MgFe) Make FS = PrFe (MgFe) Increase Y by amount 2 (Mg-DI + Fe-DI) + EN + FSIf $SiO_2 < Y$ Make Q = zeroMake $D = Y - SiO_2$ Continue with the following rules until D becomes zero If D > 0.5 (EN + FS)Make FO = 0.5 ENMake FA = 0.5 FSReduce D by amount 0.5 (EN+FS) EN becomes zero FS becomes zero Continue with rule 25 If D > TNMake PF = TNReduce D by amount TN TN becomes zero Proceed with rule 26 If D > 4 ABMake NE = ABReduce D by amount 4 AB AB becomes zero Proceed with rule 27 If D > 2 ORMake LC = ORReduce D by amount 2 OR OR becomes zero Proceed with rule 28 If D > 0.5 WOMake CS = 0.5 WOReduce D by amount 0.5 WO WO becomes zero Proceed with rule 29 If D > (Mg-DI + Fe-DI)Increase CS by an amount 0.5 (Mg-DI + Fe-DI)Increase FO by amount 0.5 (Mg-DI) Increase FA by amount 0.5 (Fe-DI) Reduce D by amount (Mg-DI+Fe-DI) Mg-DI becomes zero Fe-DI becomes zero Proceed with rule 30

30. If $D \leq 2 LC$	If $D > 2 LC$
Make~KP~=~0.5~D	Make $KP = LC$
Reduce LC by amount 0.5 D	Reduce D by amount 2 LC
D now becomes zero	LC becomes zero.
Go to rule 31.	D is the amount of over-allocated silica.
	Desilification should continue until D be-
	comes zero. This rule is so very unlikely
	to apply that no rules have been for-
	mulated. Go to 31.

31. Convert each normative mineral amount obtained by the foregoing rules to a normative mineral weight % by multiplying each mineral amount by the corresponding molecular weight given in the following list:

Q 60.08 C 101.96 Z 183.30 OR 556.64 AB 524.42 AN 278.20 LC 436.48 NE 284.10 KP = 316.32 HL = 58.44.

The total of the foregoing minerals gives the weight % of the salic group (SALIC)

AC 461.99 NS 122.06 KS 154.28 Mg-DI216.55 Fe-DI248.09 WO 116.16FS EN 100.39 131.93 FO 140.70 FA 203.78 CS 172.24 MT 231.54 CM 223.84 IL 151.75 HM 159.69 TN 196.06 PF 135.98 RU 336.21 78.08 PR 119.98 $\mathbf{C}\mathbf{C}$ 79.90 AP FR 100.09 CT 150.69 Mg-SP142.27 Fe-SP173.81

The total of the foregoing minerals gives the weight % of the femic group (FEMIC). The norm obtained will not total SALIC+FEMIC = 100 because the rock chemical analysis was used as given, and H_2O in the rock analysis was not utilized.

32. To recalculate the norm to 100% anhydrous, each of the normative minerals obtained in rule 31 should be multiplied by $\frac{100}{\text{Salic} + \text{Femic}}$. The values of Salic and Femic obtained in rule 31 can also be multiplied by the same $\frac{100}{\text{Salic} + \text{Femic}}$.

To complete the norm, HY takes the place of (EN+FS). OL the place of (FO+FA) DI the place of (Mg-DI+Fe-DI) and SP the place of (Mg-SP+Fe-SP).

- 33. The Differentiation Index (D.I.) of THORNTON and TUTTLE (1965) = Salic AN (both determined in Rule 32).
- 34. The Crystallization Index (C.I.) of POLDERVAART and PARKER (1964) = AN + Mg-DI + FO + 0.700837 (EN) + Mg-SP (all determined in rule 32).

Appendix B: Rules for calculation of the weight % norm (with biotite and hornblende)

- I. Perform rules 1 to 11 (inclusive) of the standard C.I.P.W. norm
- II. Make $CT = SnO_2$

III. If $TiO_2 \leq CaO$ Make $TN = TiO_2$ Reduce CaO by amount TN Add TN to Y TiO₂ becomes zero If $TiO_2 > CaO$ Make TN = CaOReduce TiO_2 by amount TNAdd TN to YCaO becomes zero IV. If $FeO \ge TiO_2$ Make IL = TiO_2 Reduce FeO by amount IL TiO_2 becomes zero If FeO < TiO₂ Make IL = FeO Reduce TiO₂ by amount IL FeO becomes zero Make RU = TiO₂

V. Perform rules 14 and 15 of the standard C.I.P.W. norm

VI. Either: If $Fe_2O_3 \leq 1/3$ FeO If $Na_2O \leq Fe_2O_3$ If $Na_2O > Fe_2O_3$ Make $RI = Na_2O$ Make $RI = Fe_2O_3$ Reduce Na₂O by amount RI Reduce Fe₂O₃ by amount RI Reduce FeO by amount 3 RI Reduce FeO by amount 3 RI Increase Y by amount 8 RI Increase Y by amount 8 RI Na₂O becomes zero Fe₂O₃ becomes zero Or: If $Fe_2O_3 > 1/3$ FeO If Na₂O $\leq 1/3$ FeO If $Na_2O > 1/3$ FeO Make $RI = Na_2O$ Make RI = 1/3 FeO Reduce Fe₂O₃ by amount RI Reduce Na₂O by amount RI Reduce FeO by amount 3 RI Reduce Fe₂O₃ by amount RI Increase Y by amount 8 RI Increase Y by amount 8 RI FeO becomes zero Na₂O becomes zero

- VII. Make $NS = Na_2O$. Increase Y by an amount NS
- VIII. Perform rules 19, 20 and 21 of the standard C.I.P.W. norm
 - IX. Perform rule 17 of the standard C.I.P.W. norm

X. If (MgFe) $\leq 6 \text{ OR}$ If (MgFe) > 6 ORMake Mg-BI = 1/6 (PrMg) (MgFe) Make Mg-BI = PrMg (OR) Make Fe-BI = 1/6 (PrFe) (MgFe) Make Fe-BI = PrFe (OR) Reduce OR by amount Reduce (MgFe) by amount (Mg-BI + Fe-BI)6 (Mg-BI + Fe-BI)(MgFe) becomes zero **OR** becomes zero XI. If (MgFe) $\leq 5/2$ CaO If (MgFe) > 5/2 CaO Make Mg-ACT = 1/5 PrMg (MgFe) Make Mg-ACT = 0.5 PrMg (CaO) Make Fe-ACT = 1/5 PrFe (MgFe) Make Fe-ACT = 0.5 PrFe (CaO) Reduce CaO by amount Reduce (MgFe) by amount 2 (Mg-ACT+Fe-ACT) 5 (Mg-ACT + Fe-ACT)(MgFe) becomes zero CaO becomes zero Make EN = PrMg (MgFe) Make WO = CaOMake FS = PrFe (MgFe) Increase Y by amount 8 (Mg-ACT + Fe-ACT) + WOIncrease Y by amount CaO becomes zero 8 (Mg-ACT + Fe-ACT) + EN + FSXII. If $SiO_2 \ge Y$ If $SiO_2 < Y$ Make $Q = SiO_2 - Y$ Make Q = zeroOmit rules XIII to XVI Make $D = Y - SiO_2$ Go directly to rule XVII Continue with rule XIII

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XIII. Either: If $(Mg-ACT + Fe-ACT) \ge 2 AB$ If $AB \ge D/8$ Make Mg-ED = PrMg (D/8) Make Fe-ED = PrFe(D/8)Reduce Mg-ACT by amount 2 Mg-ED Reduce Mg-ACT by amount 2 Mg-ED Reduce Fe-ACT by amount 2 Fe-ED Reduce AB by amount (Mg-ED + Fe-ED)D becomes zero. Omit rules XIV to XVI Go directly to rule XVII Or: If (Mg-ACT + Fe-ACT) < 2 ABIf $(Mg-ACT + Fe-ACT) \ge D/4$ Make Mg-ED = PrMg (D/8) Make Fe-ED = PrFe (D/8)Reduce Mg-ACT by amount 2 Mg-ED Reduce AB by amount Reduce Fe-ACT by amount 2 Fe-ED Reduce AB by amount (Mg-ED + Fe-ED)D becomes zero

- Omit rules XIV to XVI Go directly to rule XVII
- XIV. If $D \leq 0.5 (EN + FS)$ Make FO = PrMg(D)Make FA = PrFe(D)Reduce EN by amount 2 FO Reduce FS by amount 2 FA D becomes zero. Omit rules XV to XVI. Go directly to rule XVII
- XV. Either: If $(FO + FA) \leq 0.5 C$ If $(FO + FA) \ge D$ Increase Mg-SP by amount 2 PrMg (D) Increase Mg-SP by amount 2 FO Increase Fe-SP by amount 2 PrFe (D) Reduce C by amount 2 D Reduce FO by amount PrMg (D) Reduce FA by amount PrMg (D) D becomes zero. Omit rule XVI Go directly to rule XVII

Or: If (FO + FA) > 0.5 CIf $C \ge 2 D$ Increase Mg-SP by amount 2 PrMg (D) Increase Mg-SP by amount 2 PrMg (C) Increase Fe-SP by amount 2 PrFe (D) Reduce C by amount 2 D Reduce FO by amount PrMg (D) Reduce FA by amount PrFe (D) D become zero. Omit rule XVI Go directly to rule XVII.

If AB < D/8Make Mg-ED = PrMg (AB) Make Fe-ED = PrFe(AB)Reduce Fe-ACT by amount 2 Fe-ED Reduce D by amount 8 (Mg-ED + Fe-ED)AB becomes zero Continue with rule XIV

If (Mg-ACT + Fe-ACT) < D/4Make Mg-ED = 0.5 Mg-ACT Make Fe-ED = 0.5 Fe-ACT (Mg-ED + Fe-ED)Reduce D by amount 8(Mg-ED + Fe-ED)Mg-ACT becomes zero Fe-ACT becomes zero Continue with rule XIV

If D > 0.5 (EN + FS)Make FO = 0.5 ENMake FA = 0.5 FSReduce D by amount 0.5 (EN + FS)EN becomes zero. FS becomes zero Continue with rule XV

If (Fo + FA) < DIncrease Fe-SP by amount 2 FA Reduce C by amount 2(FO + FA)Reduce D by amount (FO + FA)FO becomes zero FA becomes zero Continue with rule XVI

If C > 2 D

Increase Fe-SP by amount 2 PrFe (C) Reduce D by amount 0.5 C Reduce FO by amount 0.5 PrMg (C) Reduce FA by amount 0.5 PrFe (C) C becomes zero Continue with rule XVI.

XVI. If $D \leq 4 AB$	If $D > 4 AB$
Make NE = $D/4$	Make NE = AB
Reduce AB by amount D/4	Reduce D by amount 4 AB
D becomes zero. Proceed with rule	AB becomes zero.
XVII	There are no further rules for desilifica-
	tion. The D remaining is the excess SiO_2
	over-allocated. This rule is very unlikely
	to apply.
	Go to rule XVII.

XVII. Convert each normative mineral amount obtained by the foregoing rules to a normative mineral weight % by multiplying each mineral amount by the corresponding molecular weight given in rule 31 of the standard C.I.P.W. norm. The following are the additional molecular weights required in the Femic group.
Mg-BI 798.50 Fe-BI 987.74 Mg-ACT 794.35 Fe-ACT 952.05 Mg-ED 1632.48 Fe-ED 1947.88 RI 917.87

Salic is exactly as in rule 31. Femic includes the above minerals in addition to those of rule 31.

XVIII. Recalculate the norm to 100% anhydrous and make HY, OL and SP as in rule 32. In addition make BI = (Mg-BI+Fe-BI), ACT = (Mg-ACT+Fe-ACT), ED = (Mg-ED+Fe-ED), and finally hornblende (HO) = ACT+ED+RI. The D.I. and C.I. should not be calculated from this norm variation but only from the standard C.I.P.W. norm.

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